

031: $\sqrt{2} \cdot \sin \frac{7\pi}{8} \cdot \cos \frac{7\pi}{8} = \frac{(2\sqrt{2})}{2} \cdot \sin \frac{7\pi}{8} \cdot \cos \frac{7\pi}{8} = \frac{\sqrt{2}}{2} \cdot \sin(2 \cdot \frac{7\pi}{8}) = \frac{\sqrt{2}}{2} \sin(\frac{7\pi}{4}) =$
 $= \frac{\sqrt{2}}{2} \cdot (-\frac{\sqrt{2}}{2}) = -\frac{1}{2} = -0,5$



043: $\sin 3\alpha \cos 2\alpha + \sin 2\alpha \cos 3\alpha = \sin 3\alpha \cos \alpha + \cos 3\alpha \cdot \sin 2\alpha =$
 $= \sin(3\alpha + 2\alpha) = \sin 5\alpha + \sin(11\alpha + 5\alpha) = \sin 5\alpha - \sin 5\alpha = 0$

035: $\frac{15}{\sin^2 39 + \cos^2 39} + 1 = \frac{15}{1} + 1 = 16$ $\sin 129^\circ = \sin(180^\circ - 51^\circ) = \sin 51^\circ$
 $\sin(90^\circ + 39^\circ) = \cos 39^\circ$

048: $\frac{2}{\sin \frac{\pi}{4} \cos \alpha + \cos \frac{\pi}{4} \sin \alpha + 3} = \frac{2}{\sin(\frac{\pi}{4} + \alpha)}$

Наибольшее значение, если знаменатель
 будет наименьшим, т.е. $\frac{\sqrt{2}}{2} (\cos \alpha + \sin \alpha)$ $\Rightarrow$
 $[-1, 1] \quad [-1, 1]$

Ответ $\frac{\sqrt{2}}{2} (\cos \alpha + \sin \alpha) = \frac{\sqrt{2}}{2} \cdot (\frac{\sqrt{2}}{2} + \frac{\sqrt{2}}{2}) =$
 $= \frac{\sqrt{2} \cdot 2 \cdot \sqrt{2}}{2 \cdot 2} = 1$

$\cos \alpha = \frac{1}{2} \quad \cos \frac{\pi}{4} = \frac{\sqrt{2}}{2}$
 $\sin \alpha = \frac{\sqrt{3}}{2} \quad \sin \frac{\pi}{4} = \frac{\sqrt{2}}{2}$

$\frac{2}{1+3} = \frac{2}{4} = \frac{1}{2} = 0,5$

044: $\cos^2 \frac{\alpha}{2} = \frac{1 + \cos \alpha}{2} = \frac{1 - \frac{7}{25}}{2} = \frac{\frac{18}{25}}{2} = \frac{9}{25}$
 $\cos \frac{\alpha}{2} = \sqrt{\frac{9}{25}} = \frac{3}{5} = 0,6$

$2 \cos \alpha = 1 + \cos 2\alpha$

$\frac{\pi}{4} < \frac{\alpha}{2} < \frac{\pi}{2}$

