

$$F(x) = \begin{cases} 0; & \text{при } x < 0 \\ A * \left(x - \frac{1}{2} \sin(2x) \right); & \text{при } 0 \leq x \leq \pi \\ 1; & \text{при } x > \pi \end{cases} - \text{функция распределения должна быть}$$

непрерывна, значит

$$F(0) = 0 = A * \left(0 - \frac{1}{2} \sin(2 * 0) \right) = A * \left(0 - \frac{1}{2} \sin(0) \right) = A * (0 - 0) = 0 - \text{истинно при любых } A$$

$$F(\pi) = 1 = A * \left(\pi - \frac{1}{2} \sin(2 * \pi) \right) = A * \left(\pi - \frac{1}{2} \sin(0) \right) = A * \pi = 1 - \text{истинно при } A = \frac{1}{\pi}$$

ответ 1: $A = \frac{1}{\pi}$

$$F(x) = \begin{cases} 0; & \text{при } x < 0 \\ \frac{1}{\pi} * \left(x - \frac{1}{2} \sin(2x) \right); & \text{при } 0 \leq x \leq \pi \\ 1; & \text{при } x > \pi \end{cases}$$

$$f(x) = F'(x) = \begin{cases} 0; & \text{при } x < 0 \\ \frac{1}{\pi} * (1 - \cos(2x)); & \text{при } 0 \leq x \leq \pi \\ 0; & \text{при } x > \pi \end{cases} - \text{функция плотности распределения}$$

это ответ 2)

$$MX = \int_{-\infty}^{\infty} x * f(x) * dx = \int_{-\infty}^0 x * f(x) * dx + \int_0^{\pi} x * f(x) * dx + \int_{\pi}^{\infty} x * f(x) * dx =$$

$$= \int_{-\infty}^0 x * 0 * dx + \int_0^{\pi} x * \frac{1}{\pi} * (1 - \cos(2x)) * dx + \int_{\pi}^{\infty} x * 0 * dx = \frac{1}{\pi} \int_0^{\pi} x dx - \frac{1}{\pi} \int_0^{\pi} x * \cos(2x) * dx = I_1 - I_2$$

$$I_1 = \frac{1}{\pi} \int_0^{\pi} x dx = \frac{1}{\pi} \left(\frac{x^2}{2} \right) \Big|_{x=0}^{\pi} = \frac{1}{\pi} \left(\frac{\pi^2}{2} \right) - \frac{1}{\pi} \left(\frac{0^2}{2} \right) = \frac{\pi}{2}$$

$$I_2 = \frac{1}{\pi} \int_0^{\pi} x * \cos(2x) * dx = \left[\begin{array}{l} \frac{1}{\pi} x = u; \cos(2x) dx = dv \\ du = \frac{1}{\pi} dx; v = \frac{1}{2} \sin(2x) \end{array} \right] \left[\int u dv = uv - \int v du \right] =$$

$$= \left(\frac{1}{\pi} x * \frac{1}{2} \sin(2x) \right) \Big|_0^{\pi} - \int_0^{\pi} \frac{1}{2} \sin(2x) * \frac{1}{\pi} dx = I_3 - I_4$$

$$I_3 = \left(\frac{1}{\pi} x * \frac{1}{2} \sin(2x) \right) \Big|_0^{\pi} = \left(\frac{1}{\pi} \pi * \frac{1}{2} \sin(2\pi) - \frac{1}{\pi} 0 * \frac{1}{2} \sin(2 * 0) \right) = 0$$

$$I_4 = \int_0^{\pi} \frac{1}{2} \sin(2x) * \frac{1}{\pi} dx = \frac{1}{4\pi} \int_0^{\pi} \sin(2x) d(2x) = \left(\frac{1}{4\pi} \cos(2x) \right) \Big|_{x=0}^{\pi} = \frac{1}{4\pi} \cos(2\pi) - \frac{1}{4\pi} \cos(2 * 0) = 0$$

$$I_2 = I_3 - I_4 = 0 - 0 = 0$$

$$MX = I_1 - I_2 = \frac{\pi}{2} - 0 = \frac{\pi}{2} - \text{это ответ 3)}$$

$$P\left(0 < x < \frac{\pi}{2}\right) = F\left(\frac{\pi}{2}\right) - F(0) = \frac{1}{\pi} * \left(\frac{\pi}{2} - \frac{1}{2} \sin\left(2 * \frac{\pi}{2}\right) \right) - 0 = \frac{1}{2\pi} * (\pi - \sin(\pi)) = \frac{\pi - 0}{2\pi} = 0,5 - \text{это}$$

ответ 4